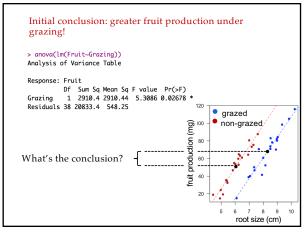
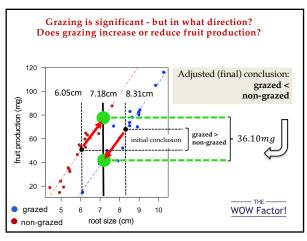
Now we can test for differences in adjusted means; but before that:

Critical statistical issues underlying General Linear Models (including ANCOVAs)

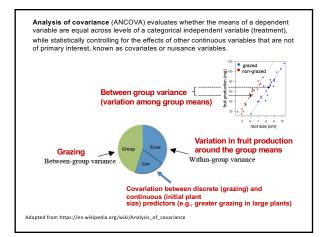
Lecture 10 (Type I and III sum-of-square)

1











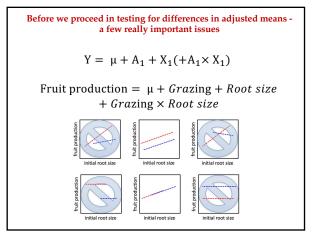
Before we proceed in testing for differences in adjusted means a few really important issues

1) Since the two main conditions hold (1) Covariate can predict the response; and 2) Groups share a common slope, i.e., interaction is not significant), we can proceed to test the effect of grazing (categorical predictor) while controlling for initial plant size (root size). Also, given that the slopes are similar, we can drop the interaction in the final analysis (thought there are discussions about whether this is cautious or not).

$$Y = \mu + A_1 + X_1 (+A_1 \times X_1)$$

Fruit production = μ + *Grazing* + *Root size*

+ Grazing × Root size



BIOL 422 & 680, Pedro Peres-Neto, Biology, Concordia University ANOVA, Regression and types of sum-of-squares

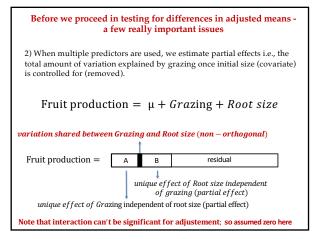


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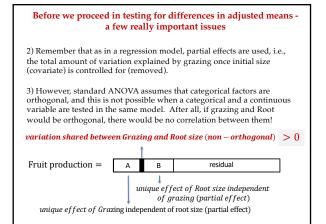
Before we proceed in testing for differences in adjusted means a few really important issues

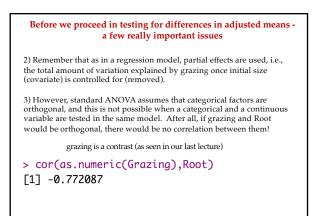
1) Since the two main conditions hold (1) Covariate can predict the response; and 2) Groups share a common slope), we can proceed to test the effect of grazing (categorical predictor) while controlling for initial plant size (root size). Also, given that the slopes are similar, we can drop the interaction in the final analysis.

2) When multiple predictors are used, we estimate partial effects i.e., the total amount of variation explained by grazing once initial size (covariate) is controlled for (removed).







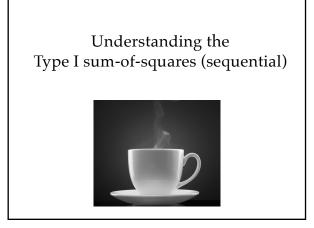


11

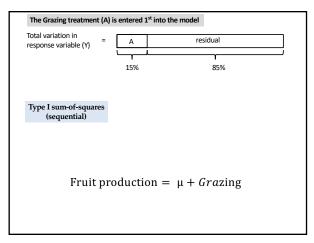
ause of lack of orthogonality between categorical (grazed/non-grazed) and ariate (initial root size), the order of the categorical and covariate change the ults when using a common ANOVA (which is based on type I Sum of squares). nova(lm(Fruit ~ Grazing+Root))		
Analysis of Variance Table		
Response: Fruit		
Df Sum Sq Mean Sq F value Pr(>F)		
Grazing 1 2910.4 2910.4 63.929 1.397e-09 ***		
Root 1 19148.9 19148.9 420.616 < 2.2e-16 ***		
Residuals 37 1684.5 45.5		
105100015 51 1001.5 15.5		
<pre>> anova(lm(Fruit ~ Root+Grazing))</pre>		
Analysis of Variance Table		
Response: Fruit		
Df Sum Sq Mean Sq F value Pr(>F)		
Root 1 16795.0 16795.0 368.91 < 2.2e-16 ***		
Grazing 1 5264.4 5264.4 115.63 6.107e-13 ***		

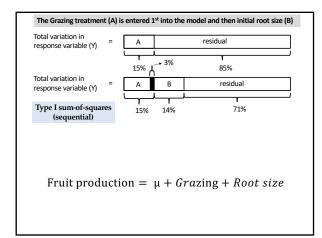
45.5

Residuals 37 1684.5

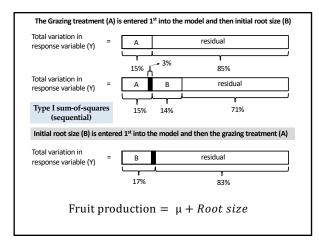


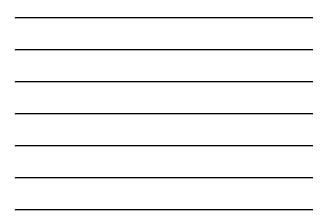


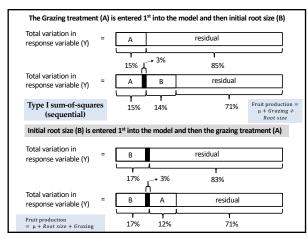






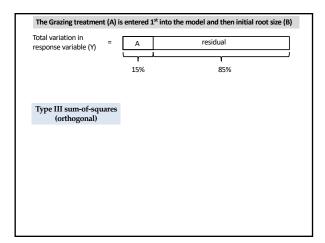




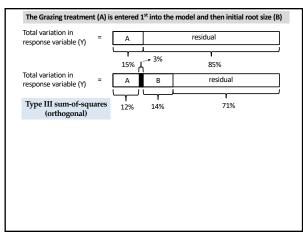


17

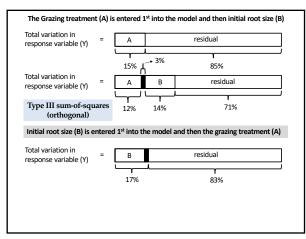
Understanding the Type III sum-of-squares (marginal or orthogonal)



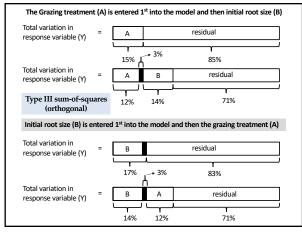


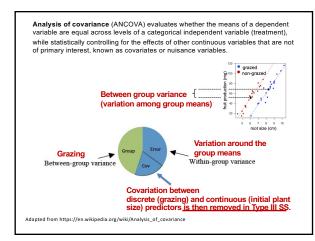


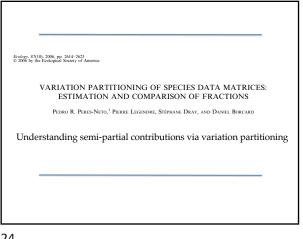


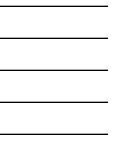












Final test: Does grazing affect fruit production once controlled for initial root size?



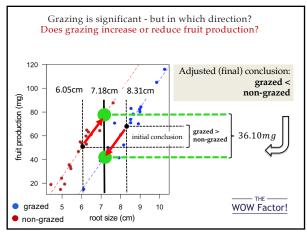


25

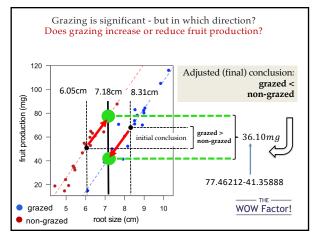
Final test: Does grazing affect fruit production once controlled for initial root size? H₀: Grazing treatments do not differ in fruit production. **H**_A: Grazing treatments differ in fruit production. > Anova(lm.Fruit, type = "III") # note "A" in Anova is capitalized Anova Table (Type III tests) Response: Fruit Sum Sq Df F value Pr(>F)
 Grazing
 5264.4
 1
 115.63
 6.107e-13

 Root
 19148.5
 1
 420.62
 2.2e-16

Grazing Residuals 1684.5 37 Type II and III Sum of squares so that order of entrance of categorical (grazing treatment) and continuous (covariate = initial root size).











2ecologia -- June 1992, Volume 90, <u>Issue 3,</u> pp 435-444 | <u>Cite as</u>

The effects of grazers on the performance of individuals and populations of scarlet gilia, *Ipomopsis aggregata*

Joy Bergelson, Michael J. Crawley

I. aggregata exhibits considerable powers of regrowth following removal of its primary shoot by herbivores, but we found no evidence of overcompensation (i.e. of significantly higher plant performance where plants were exposed to ungulate herbivory) in a comparison between individuals on grazed and ungrazed sides of exclosure fences





$Y = \mu + A_1 + X_1 + (A_1 \times X_1)$ Analysis of Covariance (ANCOVA)

Testing for assumptions should be performed before reporting results – we did not do it here so that we paid attention to the problem first!



31

Assumptions

Assumption 1: linearity (more in the regression module) The regression relationship between the dependent variable and concomitant variables must be linear.

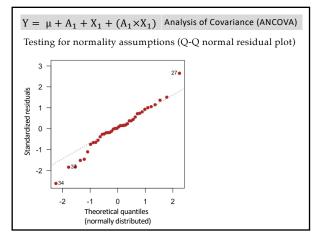
Assumption 2: homogeneity of error variances (residual plot or the Breusch-Pagan test)

Equal variances for different treatment classes and observations.

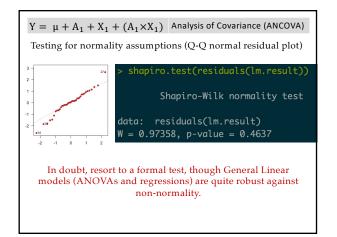
Assumption 3: independence of error terms (more in mixed models) The errors are uncorrelated. That is, the error covariance matrix is diagonal.

Assumption 4: normality of error terms (Q-Q plot) The residuals (errors) should be normally distributed.

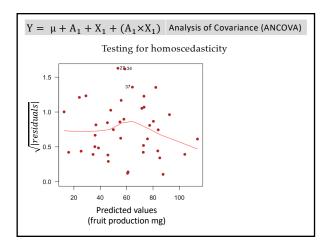
Assumption 5: homogeneity of regression slopes (tested already).

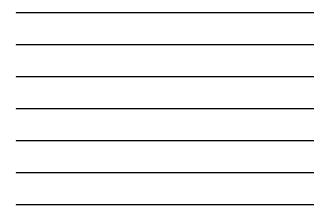


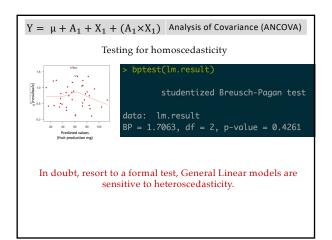




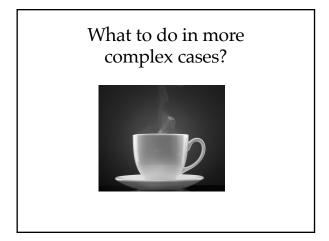




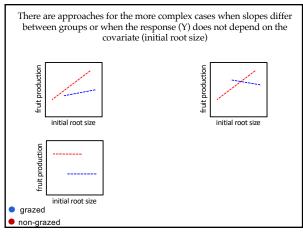


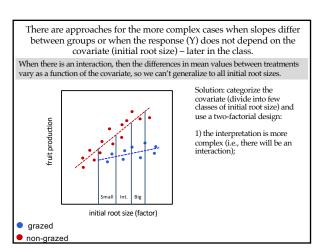




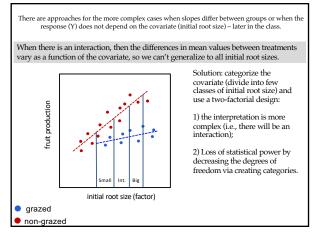




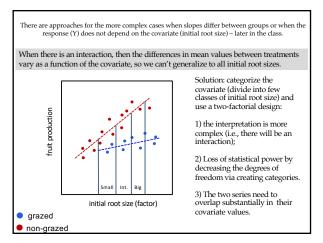




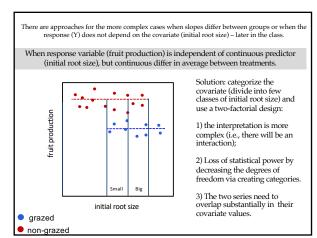












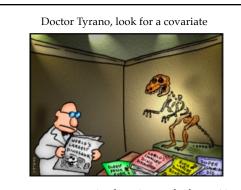
$Y = \mu + A_1 + X_1 + (A_1 \times X_1)$ Analysis of Covariance (ANCOVA)

- It is not always possible to randomize factors completely independent of each other. In the case of the fruit productivity, ideally the researchers should have made sure that the plants in grazing and no grazing plots should have had the same size.

- Confounding or nuisance (non-random) factors can often be the case, particularly in non-experimental studies.

- The terminology and some of the theory underlying "Type I, II & III" sum of squares seems to have been generated by SAS (Statistical Analysis System).

43



Doctor Tyrano, stewed in the realization that he would win no accolades for finding the world's most medium-sized dinosaur!

