

**MAST 699/MAST 833/MATH 494 Algebraic Number Theory**

**FALL 2021**

Assignment 2

Due Friday October 8

**1., 2. 3.** Marcus, Chapter 2, exercises 27-28-29

**4., 5. 6.** Marcus, Chapter 3, exercises 14-16-17

**7.** Let  $\mathfrak{a} = (2, 1 + \sqrt{-3})$  in  $\mathbb{Z}[\sqrt{-3}]$ . Show that  $\mathfrak{a} \neq (2)$  but  $\mathfrak{a}^2 = (2)\mathfrak{a}$ . Conclude that ideals do not factor uniquely into prime ideals in this ring. Why this does not contradict the theorems that we saw in class?