

```
> with(plot.s): Digits:=100: interface(dsplypreci=10): with
(Linalg):
```

```
>
```

```
N:=4;
```

```
bb:=vector(N+1, []): #for printing only = b[]
```

```
beta:=vector(N, []):
```

```
alpha:=vector(N, []):
```

```
gamma:=vector(N, []): #heights of lower ends of hanging branches
```

```
    # alpha[i]+gamma[i]<1  !!!!!!!
```

```
    #if gamma[i]>0
```

```
alpha[1]:=2/3: beta[1]:=1: gamma[1]:=1/3:
```

```
alpha[2]:=1/6: beta[2]:=2: gamma[2]:=0.0: #
```

```
alpha[3]:=2/6: beta[3]:=2.0: gamma[3]:=0: #
```

```
alpha[4]:=1/6: beta[4]:=2: gamma[4]:=5/6:
```

```
#alpha[5]:=0.5: beta[5]:=9: gamma[5]:=0:
```

```
#alpha[6]:=0.6: beta[6]:=7: gamma[6]:=0.2: #
```

```
#alpha[7]:=1.0: beta[7]:=6: gamma[7]:=0.0: #
```

```
#alpha[N]:=0.25: beta[N]:=2.4: gamma[N]:=0.75:
```

```
i:='i':
```

```
beta_const:=sum(alpha[i], i=1..N);
```

```
i:='i':
```

```
#for j from 1 to N do
```

```
#beta[j]:=beta_const;
```

```
#od:
```

```
print(`alpha =`, alpha);
```

```
print(`beta =`, beta);
```

```
print(`gamma =`, gamma);
```

```
b[1]:=0:
```

```
for j from 1 to N do
```

```
b[j+1]:=b[j]+alpha[j]/beta[j]:
```

```
  od: i:='i':
```

```
b[N+1]:=1:
```

```
ag:=vector(N, []):
```

```
al:=vector(N, []):
```

```
a:=vector(N, []):
```

```
c:=vector(N, []):
```

```
for j from 1 to N do
```

```

bb[j] := b[j];
ag[j] := bet a[j] * b[j];
al[j] := -1 + bet a[j] * b[j+1];
od:
bb[N+1] := 1:
for j from 1 to N do
a[j] := ag[j] - gamm[j];
od:

print(`b =`, bb);
print(`ag =`, ag);
print(`al =`, al);
print(`a =`, a);
print(`gamma =`, gamm);
>
>
> # ag shows maximal digit (greedy)
# al shows minimal digit (lazy) ##### if ag[j]=al[j] then j is
onto branch and there is
#
no choice there
# a shows digits assigned automatically using the vector U: U(j)
=1 lazy
#
U(j) =
0 greedy
# we can assign digit arbitrarily between minimum and maximum
and then put 2 into vector U

# Now we will name points c[i] (there is K + number of 2's in U
points c[i])
# and create a vectors si dec[], ineqc[], signc[] which shows the
character of the point c[i]
Kc:=0: # new number of c points
for j from 1 to N do if alpha[j]<1 then Kc:=Kc+1 fi od:
for j from 1 to N do if (gamm[j]>0 and alpha[j]+gamm[j]<1) then
Kc:=Kc+1 fi od:
print(`Kc =`, Kc);
c:=vector(2*N, []):
si dec:=vector(2*N, []): # 1 left (use uT), 0 right (use T)
j_of_c:=vector(2*N, []): # shows the index of the interval
associated with c

cj:=1: # this is the new index for c points
for j from 1 to N do
if (alpha[j]<1 and gamm[j]=0) then c[cj]:=b[j+1]; si dec[cj]:=

```

```

0; j_of_c[cj] := j; cj := cj + 1 fi;
if (alpha[j] < 1 and gam[j] + alpha[j] = 1) then c[cj] := b[j]; si dec
[cj] := 1; j_of_c[cj] := j; cj := cj + 1 fi;
if (gam[j] > 0 and gam[j] + alpha[j] < 1) then c[cj] := b[j]; si dec
[cj] := 1; j_of_c[cj] := j; cj := cj + 1 ;
                                c[cj] := b[j+1]; si dec[cj] := 0; j_of_c[cj] := j;
cj := cj + 1 fi;

```

```

od:
print(`c =`, c);
print(`si dec =`, si dec);
print(`j_of_c =`, j_of_c);

```

>

>

>

```

uint_of_x := x -> piecewise(x < b[2], 1, # This function needs additions
by hand for

```

```

# N9 . Automatic procedure

```

```

causes plotting problems

```

```

# but is used in other

```

```

programs

```

```

x < b[3], 2,
x < b[4], 3,
x < b[5], 4,
x < b[6], 5,
x < b[7], 6,
x < b[8], 7,
x < b[9], 8,
9);

```

```

int_of_x := x -> piecewise(x <= b[2], 1, # This function needs additions
by hand for

```

```

# N9 . Automatic procedure

```

```

causes plotting problems

```

```

# but is used in other

```

```

programs

```

```

x <= b[3], 2,
x <= b[4], 3,
x <= b[5], 4,
x <= b[6], 5,
x <= b[7], 6,

```

```

x<=b[ 8] , 7,
x<=b[ 9] , 8,
9);

x: =' x' :
uT: =x->bet a[ ui nt _of _x( x) ] * x- a[ ui nt _of _x( x) ] ;
T: =x->bet a[ i nt _of _x( x) ] * x- a[ i nt _of _x( x) ] ;
Tc: =vect or( Kc+2, [ ] ) :
for j from 1 to Kc do
if si dec[j]=0 then Tc[j]:=T( c[j] ) ;
else Tc[j]:=uT( c[j] ) fi ;
od:

pri nt ( ` Tc = ` , Tc) ;

#pl ot ( [ ' uT( x) ' , x, 0, 1, Tc[ 1] , Tc[ 2] ] , x=0. . 1, thi ckness=[ 2, 1, 1, 1, 1, 1, 1] ) ;
pl ot ( [ ' T( x) ' , x, 0, 1, Tc[ 1] , Tc[ 2] ] , x=0. . 1, thi ckness=[ 2, 1, 1, 1, 1, 1, 1, 1] ) ;

```

$$N := 4$$

$$\beta_{const} := \frac{4}{3}$$

$$\alpha =, \left[\frac{2}{3} \quad \frac{1}{6} \quad \frac{1}{3} \quad \frac{1}{6} \right]$$

$$\beta =, \left[1 \quad 2 \quad 2.0000000000 \quad 2 \right]$$

$$\gamma =, \left[\frac{1}{3} \quad 0.0000000000 \quad 0 \quad \frac{5}{6} \right]$$

$$b =, \left[0 \quad \frac{2}{3} \quad \frac{3}{4} \quad 0.9166666667 \quad 1 \right]$$

$$ag =, \left[0 \quad \frac{4}{3} \quad 1.5000000000 \quad 1.8333333333 \right]$$

$$al =, \left[-\frac{1}{3} \quad \frac{1}{2} \quad 0.8333333333 \quad 1 \right]$$

$$a =, \left[-\frac{1}{3} \quad 1.3333333333 \quad 1.5000000000 \quad 1.0000000000 \right]$$

$$\gamma =, \left[\frac{1}{3} \quad 0.0000000000 \quad 0 \quad \frac{5}{6} \right]$$

$$Kc =, 4$$

$$c =, \left[0 \quad \frac{3}{4} \quad 0.9166666667 \quad 0.9166666667 \quad c_5 \quad c_6 \quad c_7 \quad c_8 \right]$$

$$sidec =, \left[1 \ 0 \ 0 \ 1 \ sidec_5 \ sidec_6 \ sidec_7 \ sidec_8 \right]$$

$$j_of_c =, \left[1 \ 2 \ 3 \ 4 \ j_of_c_5 \ j_of_c_6 \ j_of_c_7 \ j_of_c_8 \right]$$

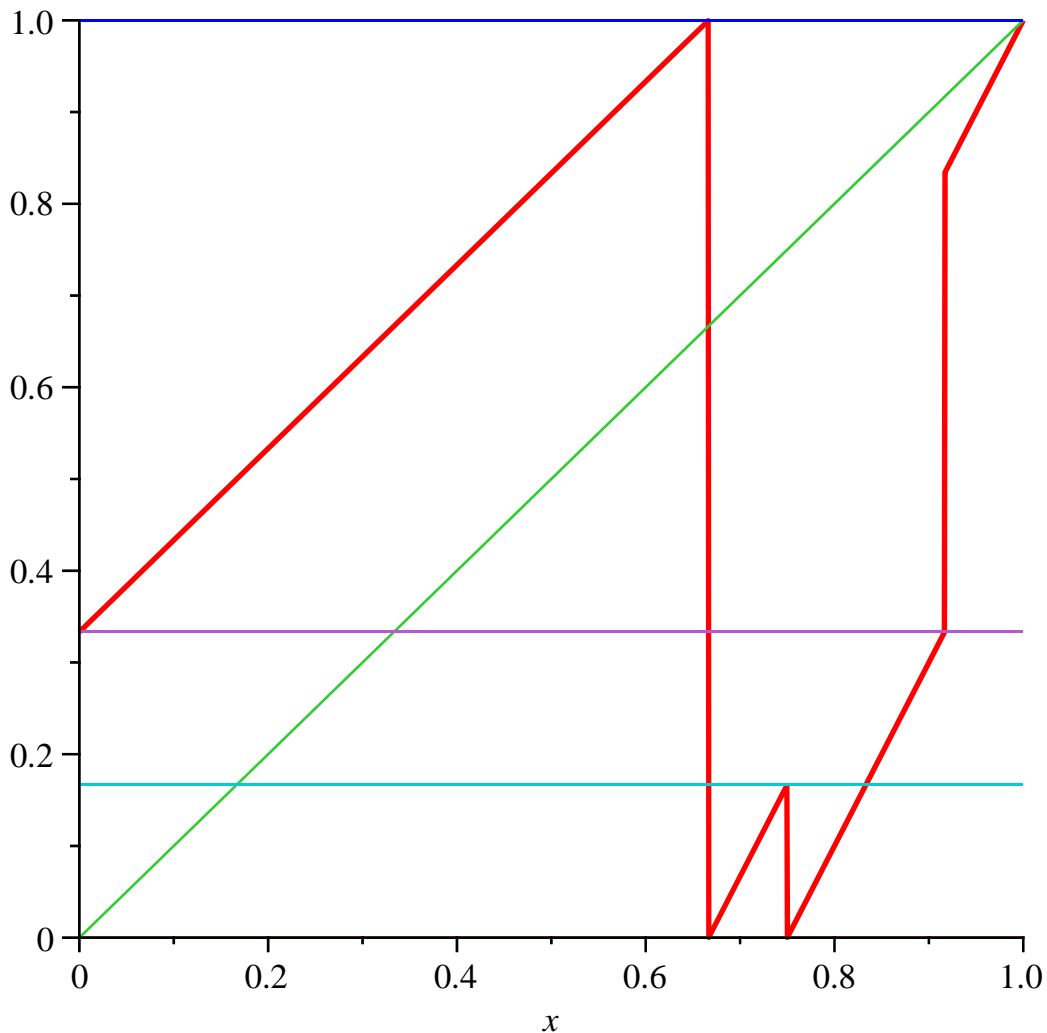
$$uint_of_x := x \rightarrow piecewise(x < b_2, 1, x < b_3, 2, x < b_4, 3, x < b_5, 4, x < b_6, 5, x < b_7, 6, x < b_8, 7, x < b_9, 8, 9)$$

$$int_of_x := x \rightarrow piecewise(x \leq b_2, 1, x \leq b_3, 2, x \leq b_4, 3, x \leq b_5, 4, x \leq b_6, 5, x \leq b_7, 6, x \leq b_8, 7, x \leq b_9, 8, 9)$$

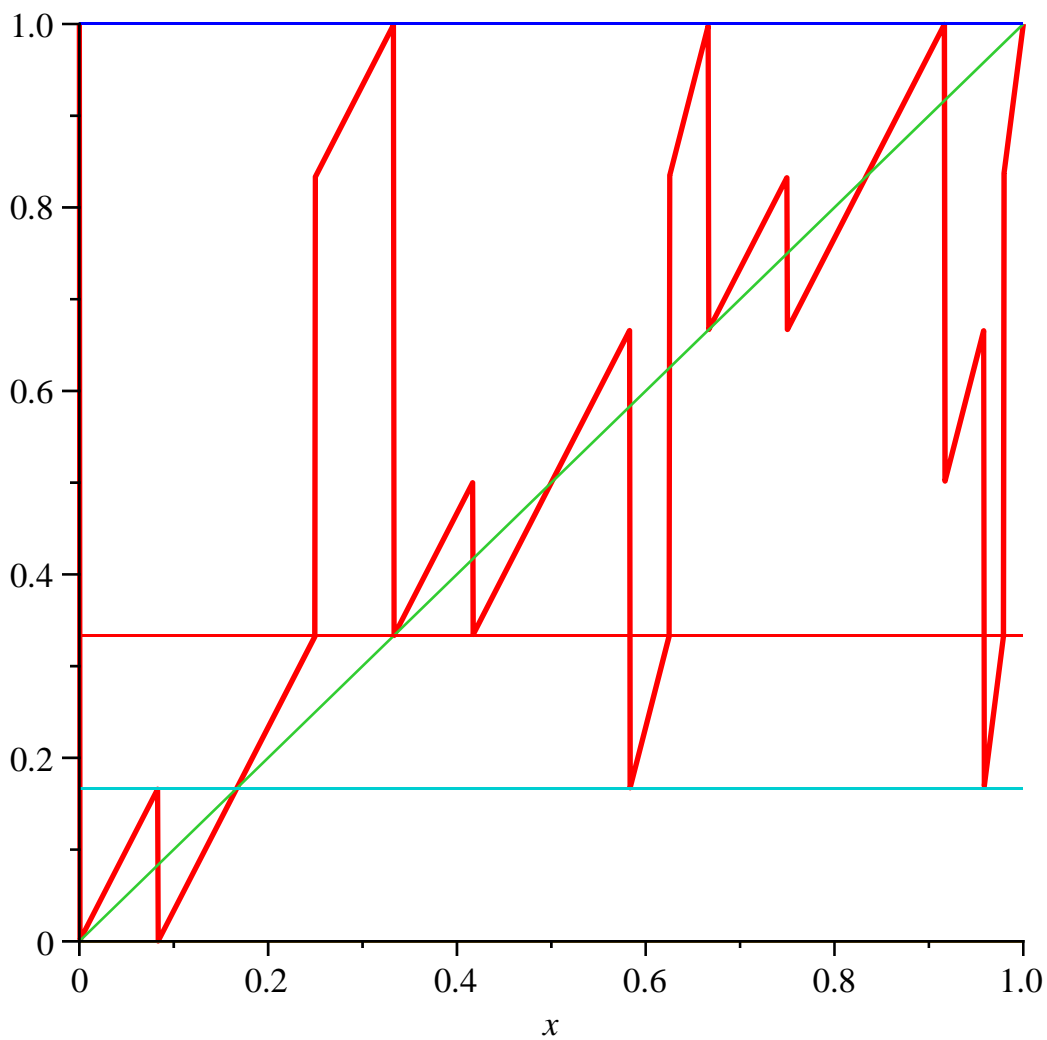
$$uT := x \rightarrow \beta_{uint_of_x(x)} x - a_{uint_of_x(x)}$$

$$T := x \rightarrow \beta_{int_of_x(x)} x - a_{int_of_x(x)}$$

$$Tc =, \left[\frac{1}{3} \ 0.1666666667 \ 0.3333333333 \ 0.8333333333 \ Tc_5 \ Tc_6 \right]$$



```
> x:=' x' :
plot ( [' T( T( T( x ) ) )' , x, 0, 1, Tc[ 1] , Tc[ 2] , Tc[ 3] ] , x=0. . 1, thickness=[ 2,
1, 1, 1, 1, 1, 1, 1, 1] );
T( T( c[ 2] ) ) ;
```



0.5000000000

(1)

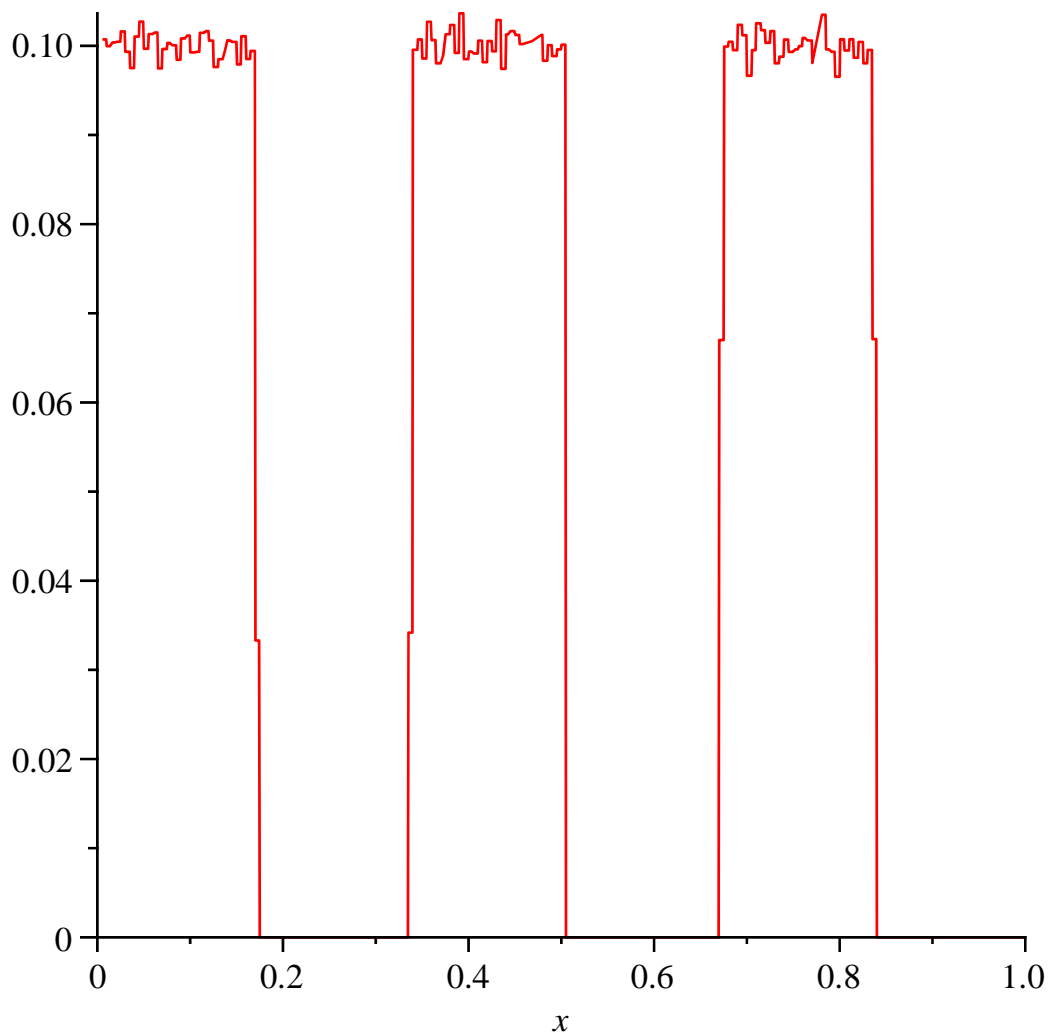
```

> niter := 500000; Nb := 200; v := array(1..Nb):
AA := 0; BB := 1:
for i from 1 to Nb do v[i] := 0; od:
y := 0.10234777777733333337:
for j from 1 to niter do
  y := T(y):
  iy := floor(Nb * (y - AA) / (BB - AA)) + 1;
  if iy > Nb then iy := Nb fi;
  v[iy] := v[iy] + 1
od:
x := 'x': g := x -> 10 * v[floor(Nb * x)] / niter;
plot(g(x), x = 0..1);

```

niter := 500000

$$g := x \rightarrow \frac{10 v_{\text{floor}(Nb \cdot x)}}{\text{niter}}$$



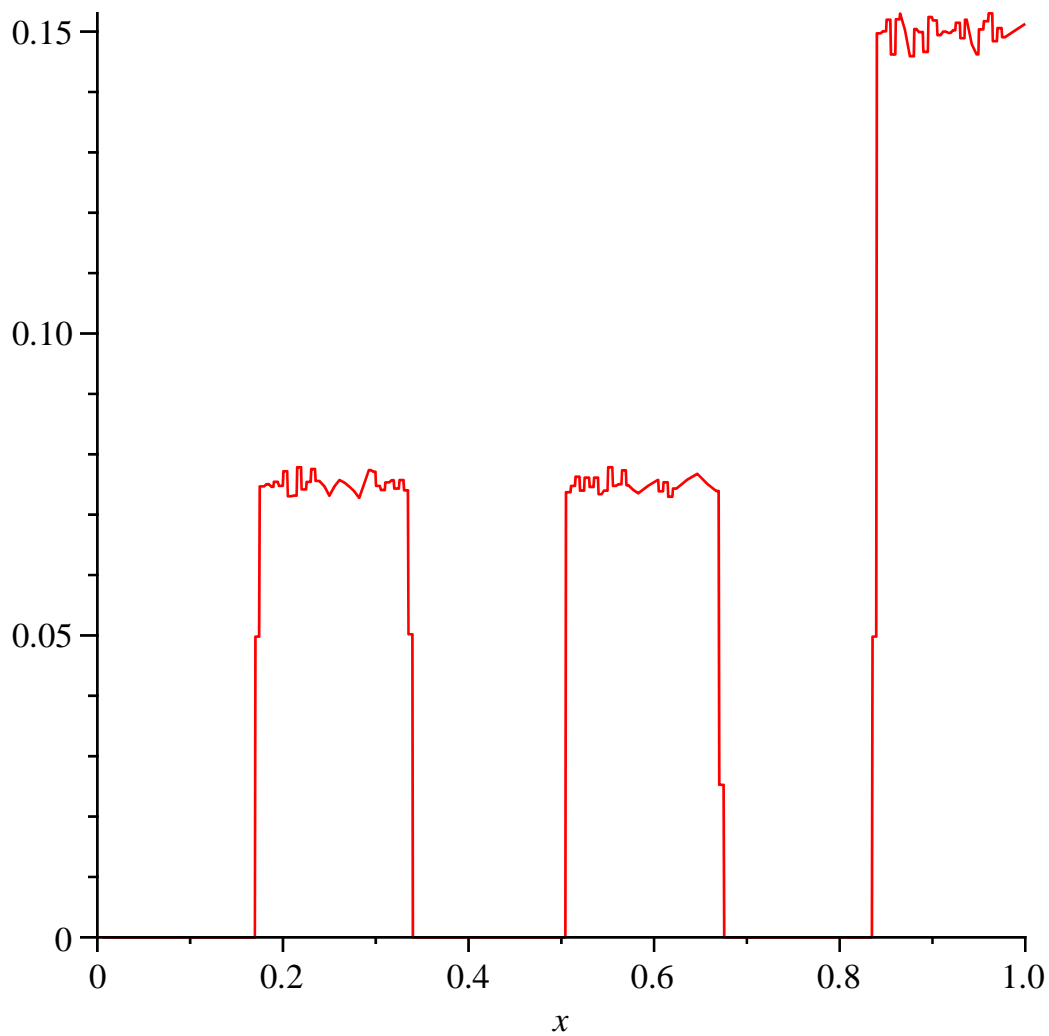
```

> niter:=500000; Nb:=200; v := array(1..Nb):
AA:=0; BB:=1:
for i from 1 to Nb do v[i]:=0; od:
y:=0.2347777777333333337:
for j from 1 to niter do
  y:=T(y):
  iy:=floor(Nb*(y-AA)/(BB-AA))+1;
  if iy>Nb then iy:=Nb fi;
  v[iy]:=v[iy]+1
od:
x:='x': g:=x->10*v[floor(Nb*x)]/niter;
plot(g(x), x=0..1);

```

niter := 500000

$$g := x \rightarrow \frac{10 v_{\text{floor}(Nb \cdot x)}}{niter}$$

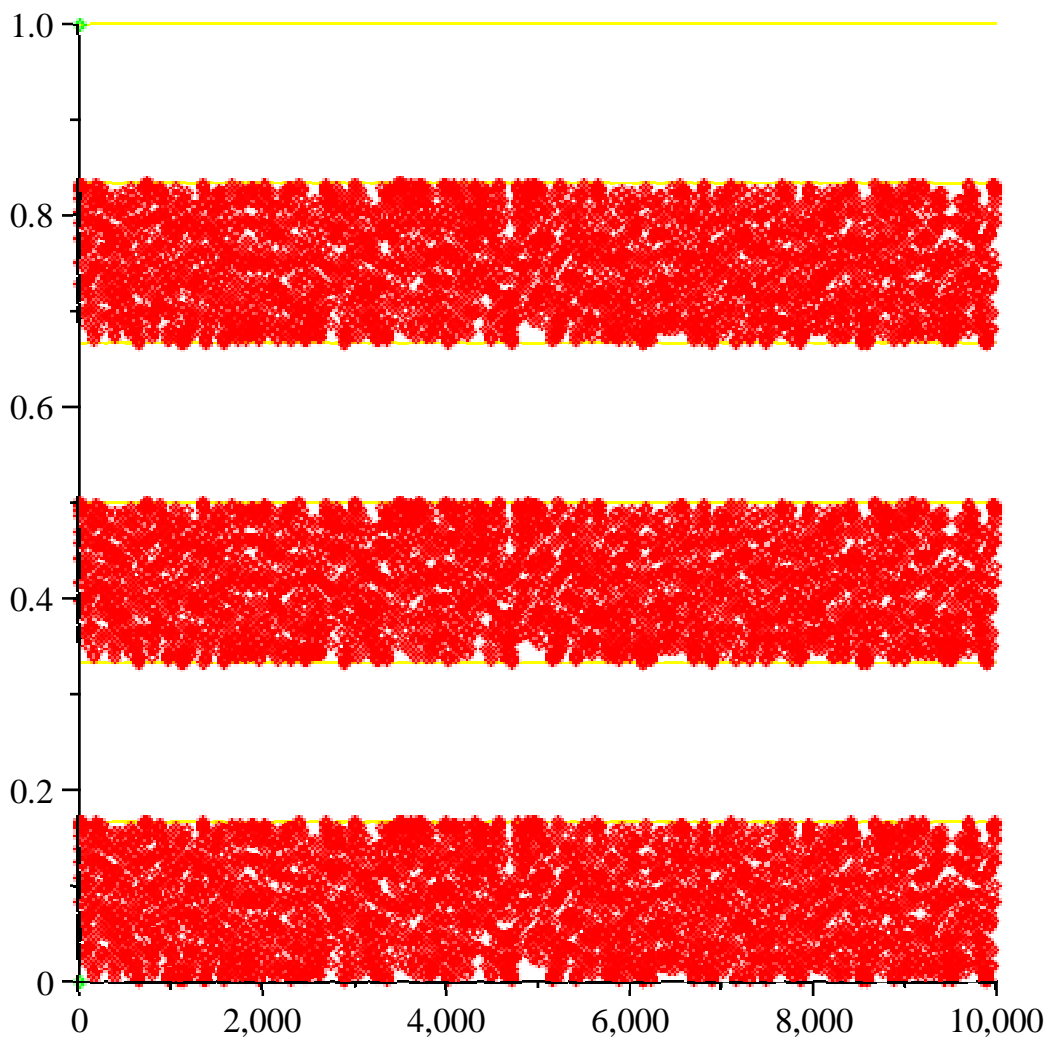


```

> x:=eval f ( rand() / 10^( 12) );
Np:=10000:
for i from 1 to Np do
px[i]:=x:
x:=T(x);
od:
y:=' y' :
pl 1:=plot ( [ 1/ 6, 2/ 6, 3/ 6, 4/ 6, 5/ 6, 6/ 6] , 0.. Np, col or =yel low) :
display(pl 1, POINTS(seq( [ i , px[ i ] ], i=1.. Np), COLOR( RGB, 1, 0, 0) ),
POINTS([0.0, 0.0], [1.0, 1.0], COLOR( RGB, 0, 1, 0) ));

```

$x := 0.3957188605$



>

> ud: =vector(50) : Digits: =100; NN: =50; #Expansion with variable
sl opes

d: =vector(50) :

xx: =0. 23777337737373737;

xxt: =xx:

bet: =1:

for i from 1 to NN do

bet: =bet / bet a[ui nt _of _x(xxt)] ;

ud[i] : =a[ui nt _of _x(xxt)] ;

udb[i] : =a[ui nt _of _x(xxt)] * bet ;

xxt: =uT(xxt) ;

od:

xxt: =xx:

bet: =1:

for i from 1 to NN do

bet: =bet / bet a[i nt _of _x(xxt)] ;

d[i] : =a[i nt _of _x(xxt)] ;

db[i] : =a[i nt _of _x(xxt)] * bet ;

xxt: =T(xxt) ;

od:

```

print ( ud ) ;
uls_it_x:=eval f ( sum( udb[ j 1] , j 1=1. . NN ) ) ;
print ( d ) ;
ls_it_x:=eval f ( sum( db[ j 1] , j 1=1. . NN ) ) ;
terr:=xx-uls_it_x;
err:=xx-ls_it_x;

```

Digits := 100

NN := 50

xx := 0.2377733774

$$\left[-\frac{1}{3}, -\frac{1}{3}, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.0000000000, 1.0000000000, 1.5000000000, -\frac{1}{3}, \right.$$

$$-\frac{1}{3}, 1.0000000000, 1.0000000000, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.0000000000,$$

$$1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.0000000000, 1.0000000000,$$

$$1.0000000000, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.5000000000, -\frac{1}{3},$$

$$-\frac{1}{3}, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.0000000000, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.5000000000,$$

$$\left. -\frac{1}{3}, -\frac{1}{3}, 1.0000000000, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.0000000000, 1.0000000000 \right]$$

uls_it_x := 0.2377733191

$$\left[-\frac{1}{3}, -\frac{1}{3}, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.0000000000, 1.0000000000, 1.5000000000, -\frac{1}{3}, \right.$$

$$-\frac{1}{3}, 1.0000000000, 1.0000000000, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.0000000000,$$

$$1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.0000000000, 1.0000000000,$$

$$1.0000000000, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.5000000000, -\frac{1}{3},$$

$$-\frac{1}{3}, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.0000000000, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.5000000000,$$

$$\left. -\frac{1}{3}, -\frac{1}{3}, 1.0000000000, 1.5000000000, -\frac{1}{3}, -\frac{1}{3}, 1.0000000000, 1.0000000000 \right]$$

ls_it_x := 0.2377733191

terr := 5.828829832 10⁻⁸

err := 5.828829832 10⁻⁸

(2)

>

>

```

> NN:=150; chi := ( x1, x2, t ) -> pi ecewi se( t <x1, 0, t <=x2, 1, 0 ) ;
uchi := ( x1, x2, t ) -> pi ecewi se( t <x1, 0, t <x2, 1, 0 ) ;

```

#Expansion of c1, c2 ... and all the S's

```

for i from 1 to Kc do
xxt:=c[i];
bet:=1:
  for n from 1 to NN+1 do
    if si dec[i]=1 then int x:=ui nt_of_x(xxt) el se int x:=
int_of_x(xxt) fi;
    bet_real:=bet;

    bet:=bet/bet a[i nt x];
    dcb[i, n]:=a[i nt x]*bet;

    if si dec[i]=0 then
      for ii from 1 to Kc do
        if xxt>c[ii]+10^(-15) then cc[i,ii,n]:=1*
bet_real el se cc[i,ii,n]:=0 fi;
        od;
        if int x=1 then Sc[i, n]:= 0
          el se Sc[i, n]:=sum(1/(bet a[j 7]), j 7=1..
int x-1)*bet_real fi;
          #bc[i, n]:=b[i nt x]*bet_real;
          #####
          el se
            for ii from 1 to Kc do
              if xxt<c[ii]-10^(-15) then cc[i,ii,n]:=1*
bet_real el se cc[i,ii,n]:=0 fi;
              od;
              if int x=N then Sc[i, n]:= 0
                el se Sc[i, n]:=sum(1/(bet a[j 8]), j 8=
int x+1..N)*bet_real fi;
                #bc[i, n]:=b[i nt x+1]*bet_real;
              fi;
              val c[i, n]:=xxt;
              bet c[i, n]:=bet_real;
              if si dec[i]=1 then
                Roundi ng:=i nf i ni t y;
                xxt:=uT(xxt)
                el se
                Roundi ng:=0;
                xxt:=T(xxt)
              fi;
              Roundi ng:=near est;

            od;
            l s_i t_x:=sum(dcb[i, j 1], j 1=1..NN);
            od;

for i from 1 to Kc do

```

```

S[i] :=eval f ( sum( Sc[ i , j 21+1] , j 21=1. . NN) );
#sum_b[i] :=eval f ( sum( bc[ i , j 2+1] , j 2=1. . NN) );
od;
for i from 1 to Kc do
for j from 1 to Kc do
SS[i , j] :=eval f ( sum( cc[ i , j , j 1+1] , j 1=1. . NN) );

#print ( `SS[`, i , j, `] =`, SS[i , j] ):
od; od:

```

$NN := 150$

$\chi := (x1, x2, t) \rightarrow \text{piecewise}(t < x1, 0, t \leq x2, 1, 0)$

$uchi := (x1, x2, t) \rightarrow \text{piecewise}(t < x1, 0, t < x2, 1, 0)$

$xxt := 0$

$bet := 1$

$Is_it_x := -5.523000043 \cdot 10^{-100}$

$xxt := \frac{3}{4}$

$bet := 1$

$Is_it_x := 0.7500000000$

$xxt := 0.9166666667$

$bet := 1$

$Is_it_x := 0.9166666667$

$xxt := 0.9166666667$

$bet := 1$

$Is_it_x := 0.9166666667$

$S_1 := 6.5000000000$

$S_2 := 1.5000000000$

$S_3 := 2.0000000000$

$S_4 := 2.0000000000$

(3)

```

MM =mat r i x( Kc, Kc, [] ):
MMM =mat r i x( Kc, Kc, [] ):
for i from 1 to Kc do
for j from 1 to Kc do

```

```

MM[i , j] :=- SS[j , i] ;
MMM[i , j] :=- SS[j , i] ;
od; od;

```

```

print(`MM = `, MM);
print(`det MM = `, det(MM));
print(1/beta[j_of_c[5]]);

```

```

print(`eigenvalues MM = `, eigenvalues(MM));
print(`1/ average beta = `, 1/ave_beta);
ve:=vector(Kc, []):
for i from 1 to Kc do
ve[i]:=1;

```

```

MMM[i, i]:=MMM[i, i]+1.0;
od:
MMM[2, 2]:=0; MMM[3, 3]:=0;
print(MMM);
print(`det MMM = `, det(MMM));
print(ve); _t:='_t';

```

```

DD:=insolve(MMM, ve);
sum((S[i 7]-1/beta[j_of_c[i 7]])*DD[i 7], i 7=1..Kc)-(1-sum
(1/beta[i 8], i 8=1..N));
eigenvalues(MM);

```

$$MM = \begin{bmatrix} -0.0000000000 & -3.0000000000 & -2.0000000000 & -0.0000000000 \\ -5.0000000000 & -1.0000000000 & -1.0000000000 & -1.0000000000 \\ -5.0000000000 & -0.0000000000 & -1.0000000000 & -2.0000000000 \\ -5.0000000000 & -0.0000000000 & -1.0000000000 & -2.0000000000 \end{bmatrix}$$

$$\det MM = , 0.0000000000$$

$$\frac{1}{\beta_{j_of_c_5}}$$

$$\text{eigenvalues } MM = , 3.7201532545, -6.7201532545, 0.0000000000, -1.0000000000$$

$$1/\text{average beta} = , \frac{1}{\text{ave_beta}}$$

$$MMM_{2,2} := 0$$

$$MMM_{3,3} := 0$$

$$\begin{bmatrix} 1.0000000000 & -3.0000000000 & -2.0000000000 & -0.0000000000 \\ -5.0000000000 & 0 & -1.0000000000 & -1.0000000000 \\ -5.0000000000 & -0.0000000000 & 0 & -2.0000000000 \\ -5.0000000000 & -0.0000000000 & -1.0000000000 & -1.0000000000 \end{bmatrix}$$

$$\det MMM = , -1.332267630 \cdot 10^{-14}$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 \end{bmatrix}$$

$$_t := _t$$

$$DD := \begin{bmatrix} -0.2000000000 & -0.4000000000 & -0.0000000000 & -0.0000000000 \end{bmatrix}$$

$$2.960594732 \cdot 10^{-16}$$

$$\left[3.7201532545, 1, \left\{ \left[0.8022929283 \quad -0.5969305296 \quad -0.5969305296 \quad -0.5969305296 \right] \right\} \right], \quad (4)$$

$$\left[0.0000000000, 1, \right.$$

$$\left. \left\{ \left[-0.0565685425 \quad 0.5656854249 \quad -0.8485281374 \quad 0.5656854249 \right] \right\}, \left[\right.$$

$$-6.7201532545, 1, \left\{ \left[0.5969305296 \quad 0.8022929283 \quad 0.8022929283 \quad 0.8022929283 \right] \right\}, \left[\right.$$

$$-1.0000000000, 1,$$

$$\left. \left\{ \left[0.1571348403 \quad 0.3142696805 \quad -0.3928371007 \quad -0.3928371007 \right] \right\} \right]$$

> **DDv := vector(4, [0.1571348403, 0.3142696805, -0.3928371007, -0.3928371007]);**

$$DDv := \begin{bmatrix} 0.1571348403 & 0.3142696805 & -0.3928371007 & -0.3928371007 \end{bmatrix} \quad (5)$$

> **MMM := matrix(4, 4, [[1, -3, -2, 0], [-5, 0, -1, -1], [-5, 0, 0, -2], [-5, 0, -1, -1]]);**

vi := vector(4, [0, 0, 0, 0]);

linsolve(MMM, vi); #for more general form of invariant density

$$MMM_i := \begin{bmatrix} 1 & -3 & -2 & 0 \\ -5 & 0 & -1 & -1 \\ -5 & 0 & 0 & -2 \\ -5 & 0 & -1 & -1 \end{bmatrix}$$

$$vi := \begin{bmatrix} 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} -t_1 & 2-t_1 & -\frac{5}{2}-t_1 & -\frac{5}{2}-t_1 \end{bmatrix}$$

(6)

> **density := proc(t) local j, i, den;**

i := 'i':

#den := sum(chi(b[i], b[i+1], t) / beta[i], i = 1..N);

den := 0:

```

    for j from 1 to Kc do
    if sidec[j]=0 then
        den:=den+ DDv[j] * sum( ( chi ( 0, val c[j, i 1+1], t) ) *
bet c[j, i 1+1], i 1=1..150) fi;

        if sidec[j]=1 then
            den:=den+ DDv[j] * sum( ( uchi ( val c[j, i 1+1], 1, t) ) *
bet c[j, i 1+1], i 1=1..150) fi;

        od;
    return den;
end proc;

```

#Normalizing factor

```

NC:=0:
for j from 1 to Kc do
if sidec[j]=0 then
    NC:=NC+DDv[j] * sum( ( val c[j, i 1+1] ) * bet c[j, i 1+1], i 1=1..50) fi;
if sidec[j]=1 then
    NC:=NC+DDv[j] * sum( ( 1- val c[j, i 1+1] ) * bet c[j, i 1+1], i 1=1..50) fi;

od:

print(`NC = `, NC);

plot ( [ ( 1/ NC) * densi t y( t ) ], t=0..1-0.000001, col or=bl ack, t hi ckness=
2);

```

density := **proc**(*t*)

local *j, i, den*;

i := 'i';

den := 0;

for *j* **to** *Kc* **do**

if *sidec*[*j*]=0 **then**

den := *den* + *DDv*[*j*] * (sum(chi(0, *valc*[*j, il + 1*], *t*) * *betc*[*j, il + 1*], *il* = 1
..150))

end if;

if *sidec*[*j*]=1 **then**

den := *den* + *DDv*[*j*] * (sum(*uchi*(*valc*[*j, il + 1*], 1, *t*) * *betc*[*j, il + 1*], *il* = 1
..150))

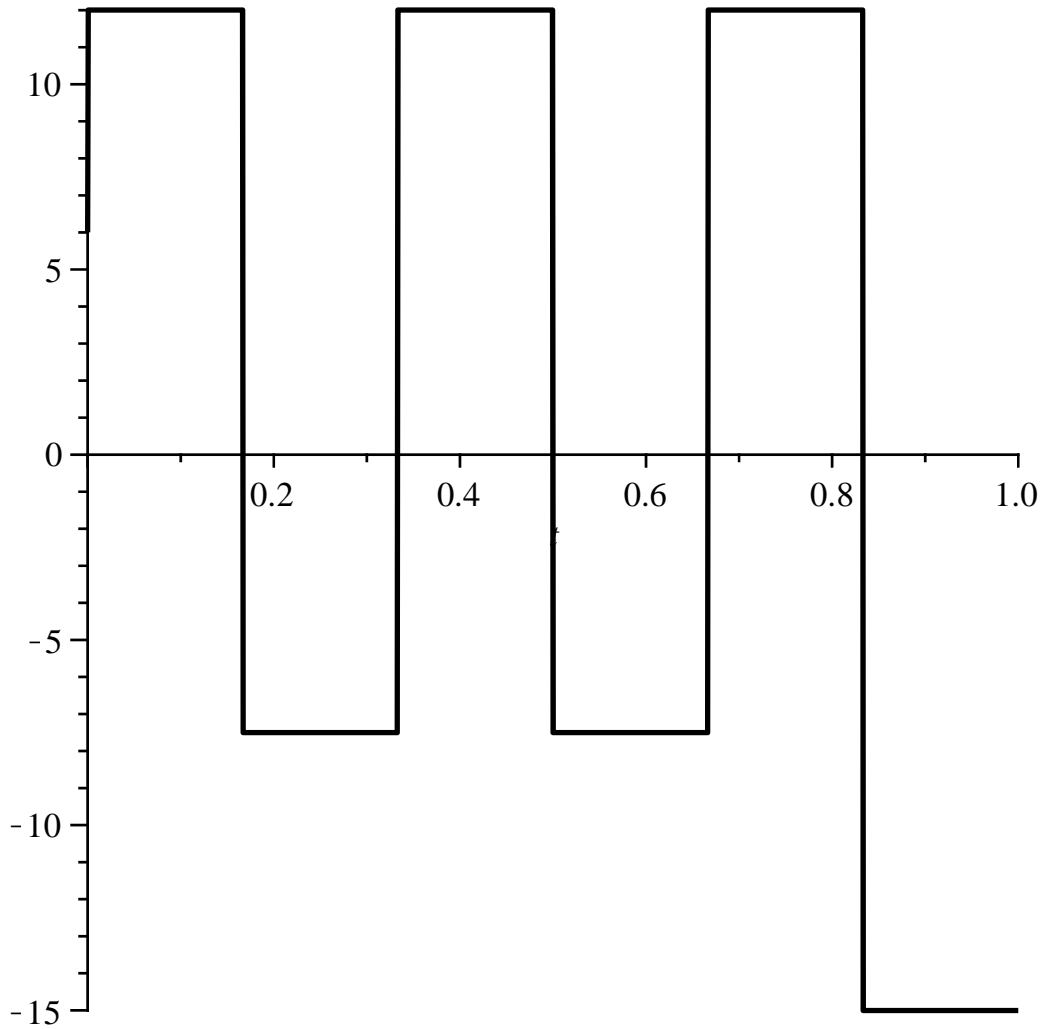
end if

end do;

```
return den
```

```
end proc
```

```
NC = , 0.0261819969
```



```
>
```

```
>
```

```
#check density
```

```
#preimages
```

```
for j6 from 0 to 9 do
```

```
  y[j6] := j6/10 + (0.1) * rand() / 10^12;
```

```
od;
```

```
for j6 from 0 to 9 do
```

```
  for i3 from 1 to N do
```

```
    pre[i3] := (y[j6] + a[i3]) / beta[i3];
```

```
  od;
```

```
  plot([T(t), 0, 1, y[j6]], t=0..1,
```

```
  color=[red, black, black, yellow]);
```

```
  su:=0;
```

```
  for i3 from 1 to N do
```

```
    if (pre[i3] >= b[i3] and pre[i3] <= b[i3+1]) then
```

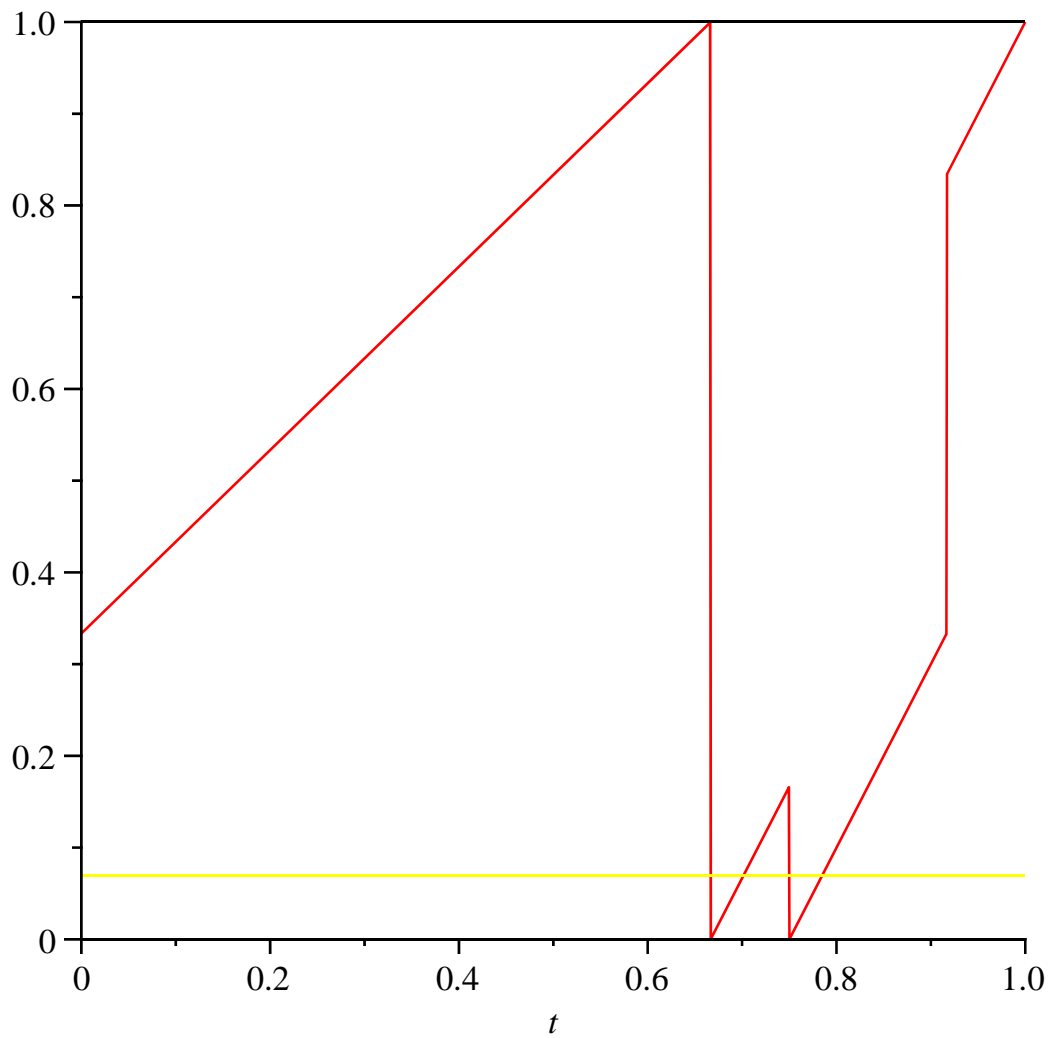
```
      su := su + evalf(density(pre[i3]) / beta[i3]);
```

```
    print(i3);
```



```
fi;  
od;  
err[j6]:=eval f(densit y(y[j6]) - su);  
od;
```

```
for j6 from 0 to 9 do  
print(`y =`, y[j6]);  
print(`err[`, j6, `]=`, err[j6]);  
od;
```

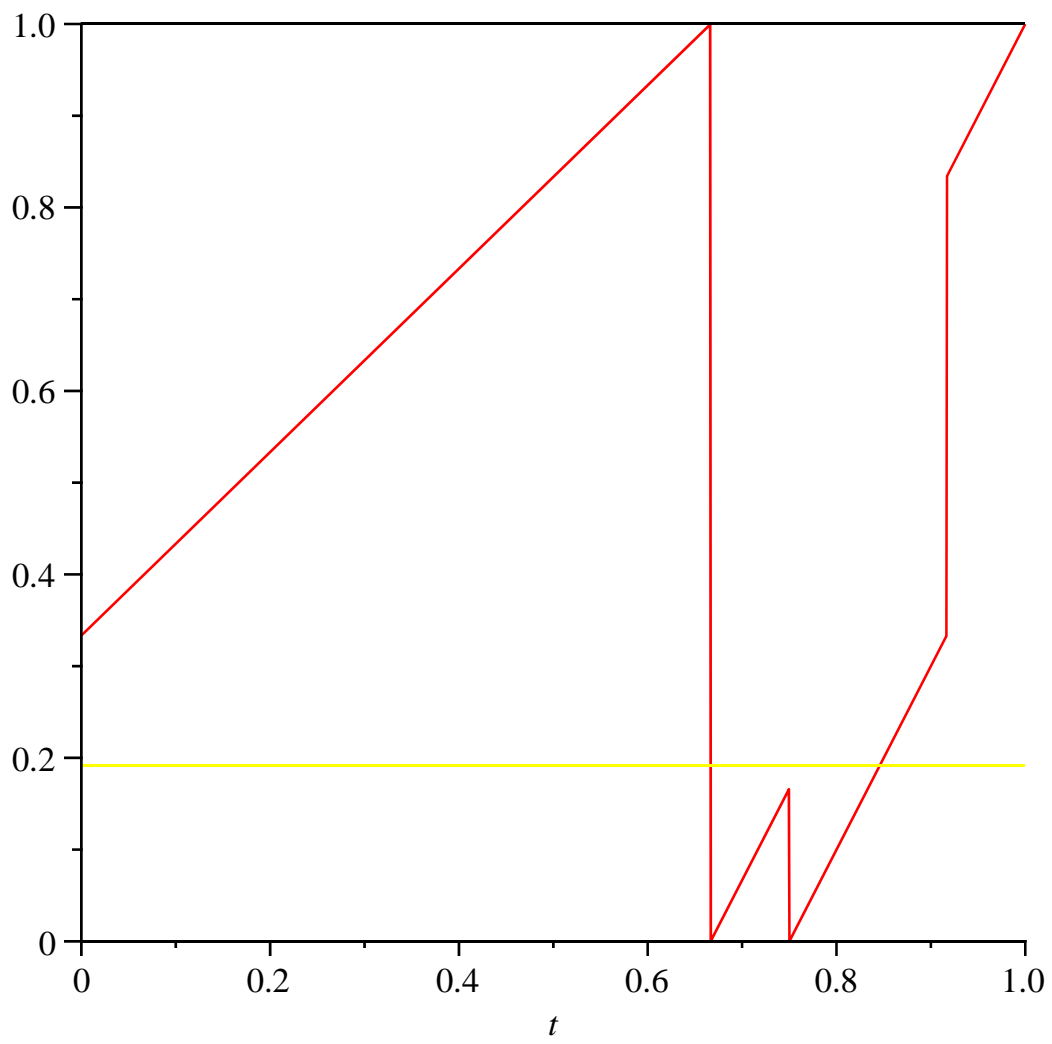


$su := 0$

2

3

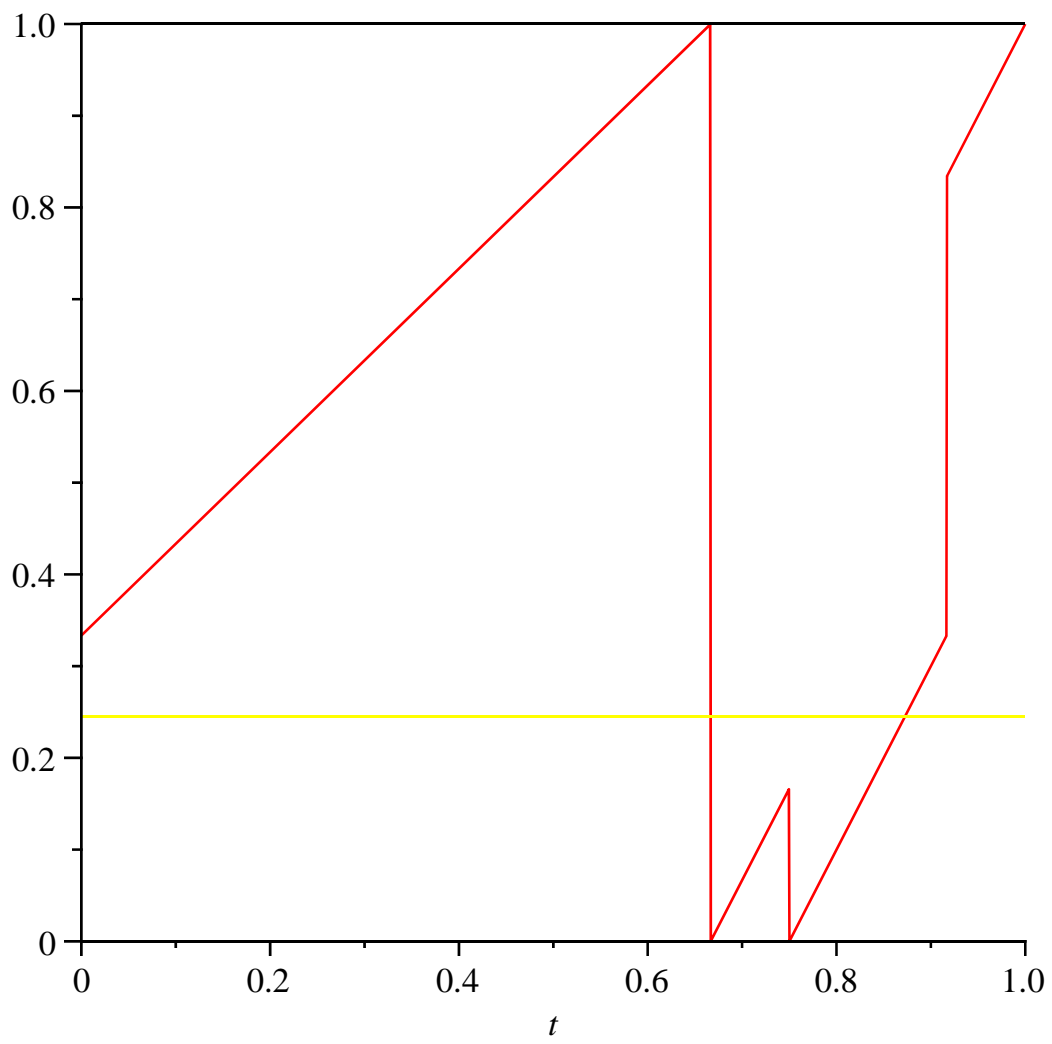
$err_0 := -2.000003489 \cdot 10^{-10}$



$su := 0$

3

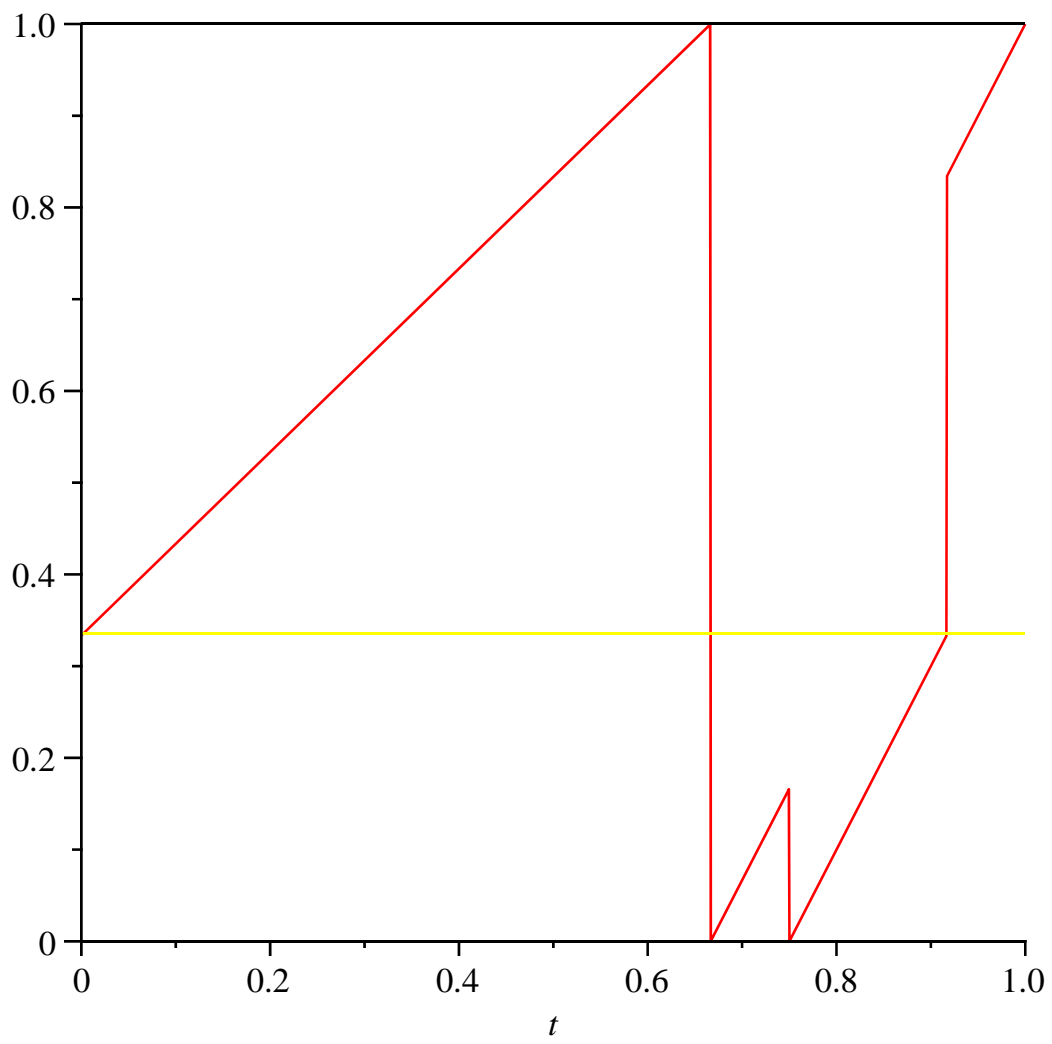
$err_1 := -1.500005234 \cdot 10^{-10}$



$su := 0$

3

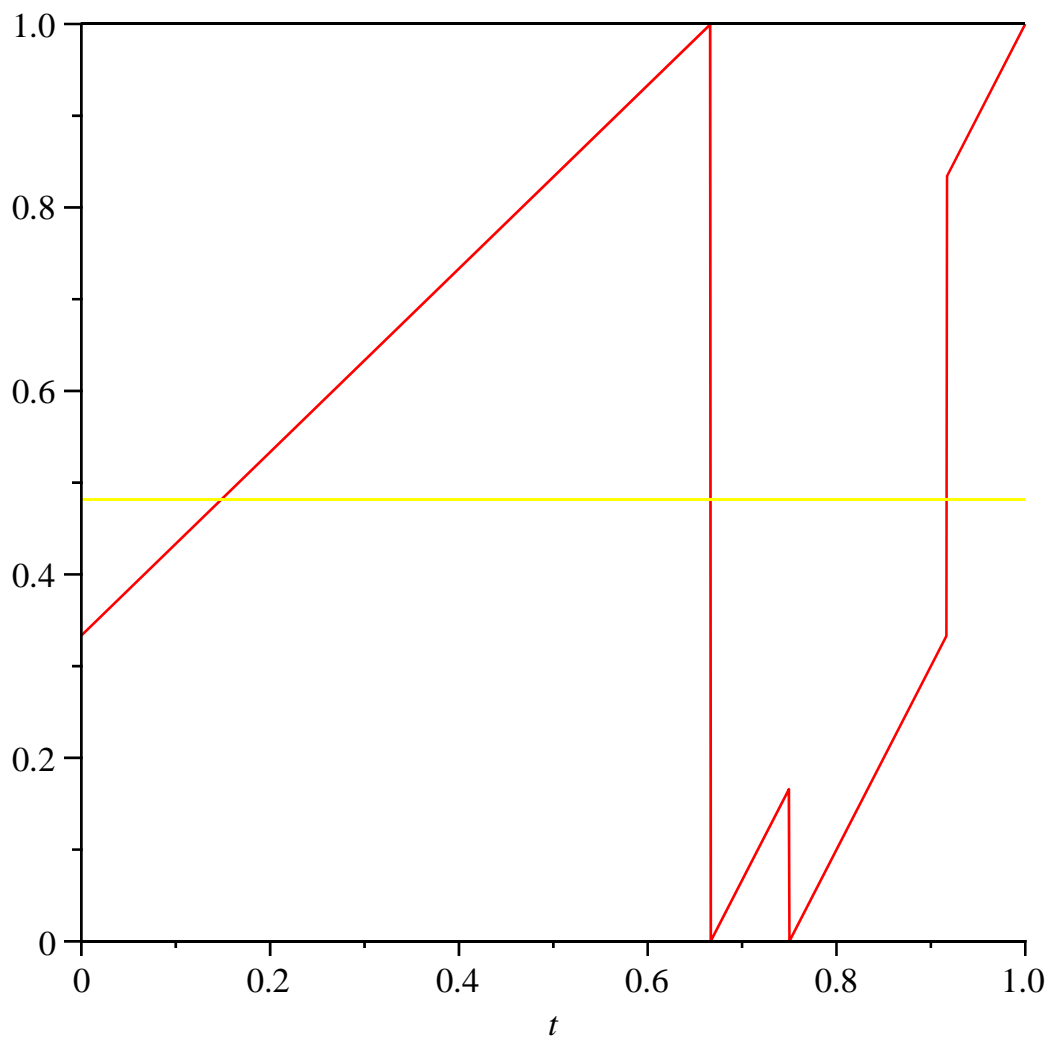
$err_2 := -1.500005234 \cdot 10^{-10}$



$su := 0$

1

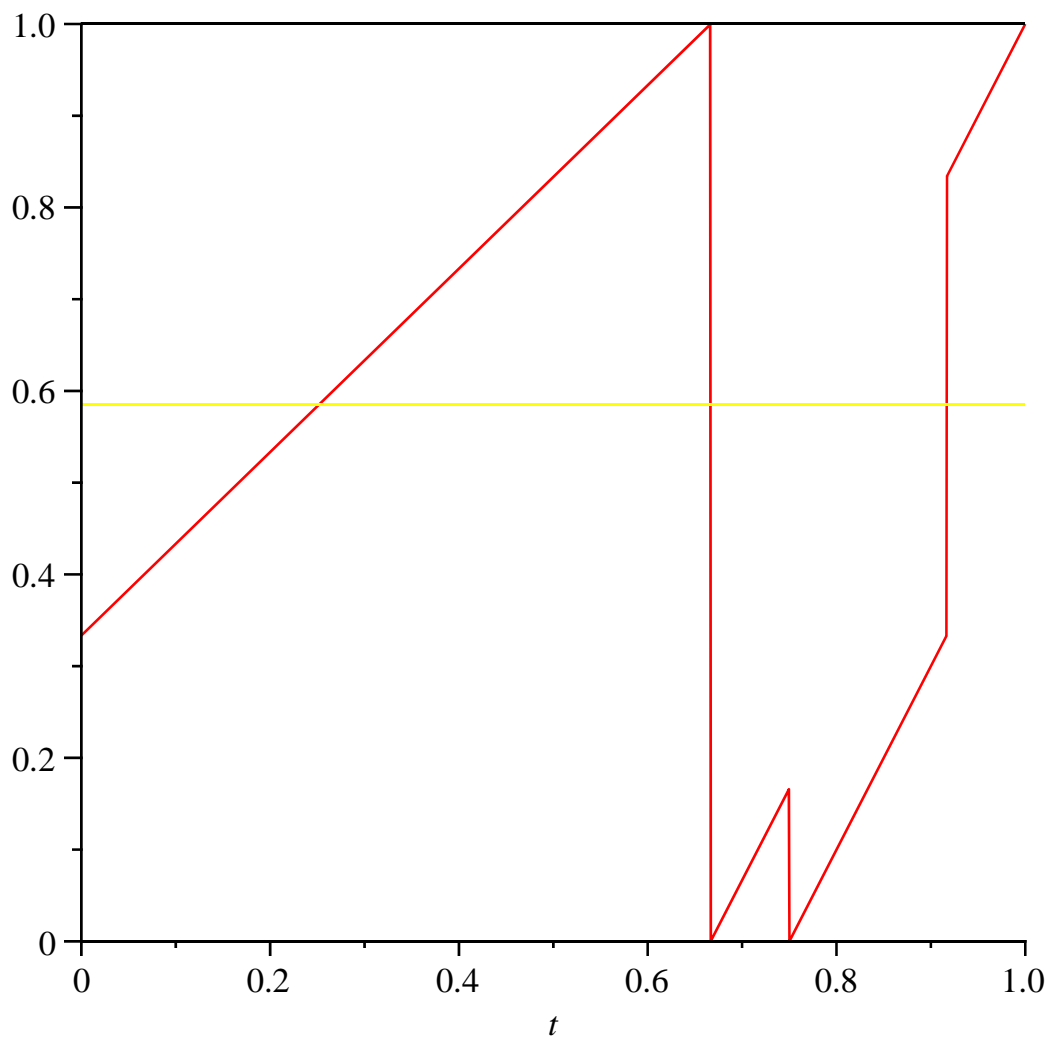
$err_3 := 1.000001745 \cdot 10^{-10}$



$su := 0$

1

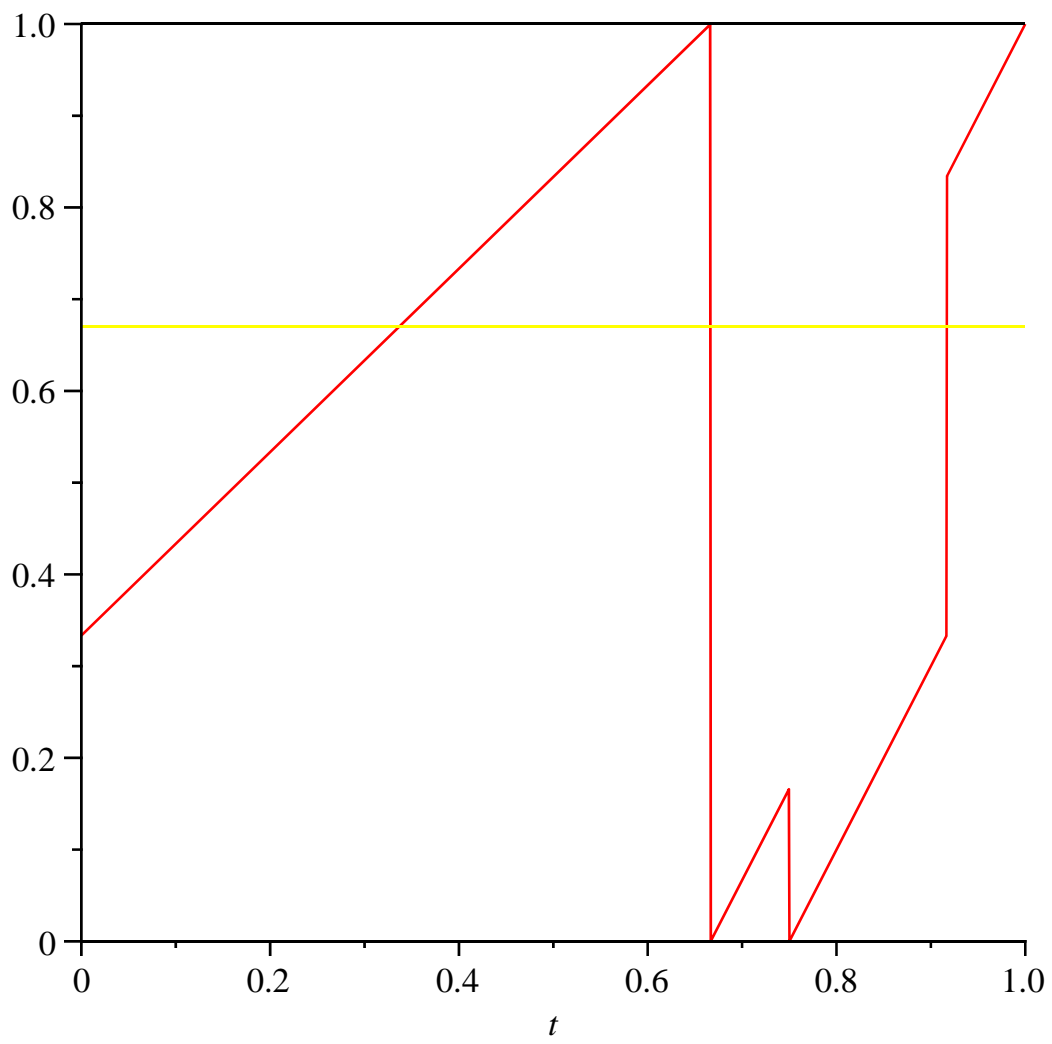
$err_4 := 1.000001745 \cdot 10^{-10}$



$su := 0$

1

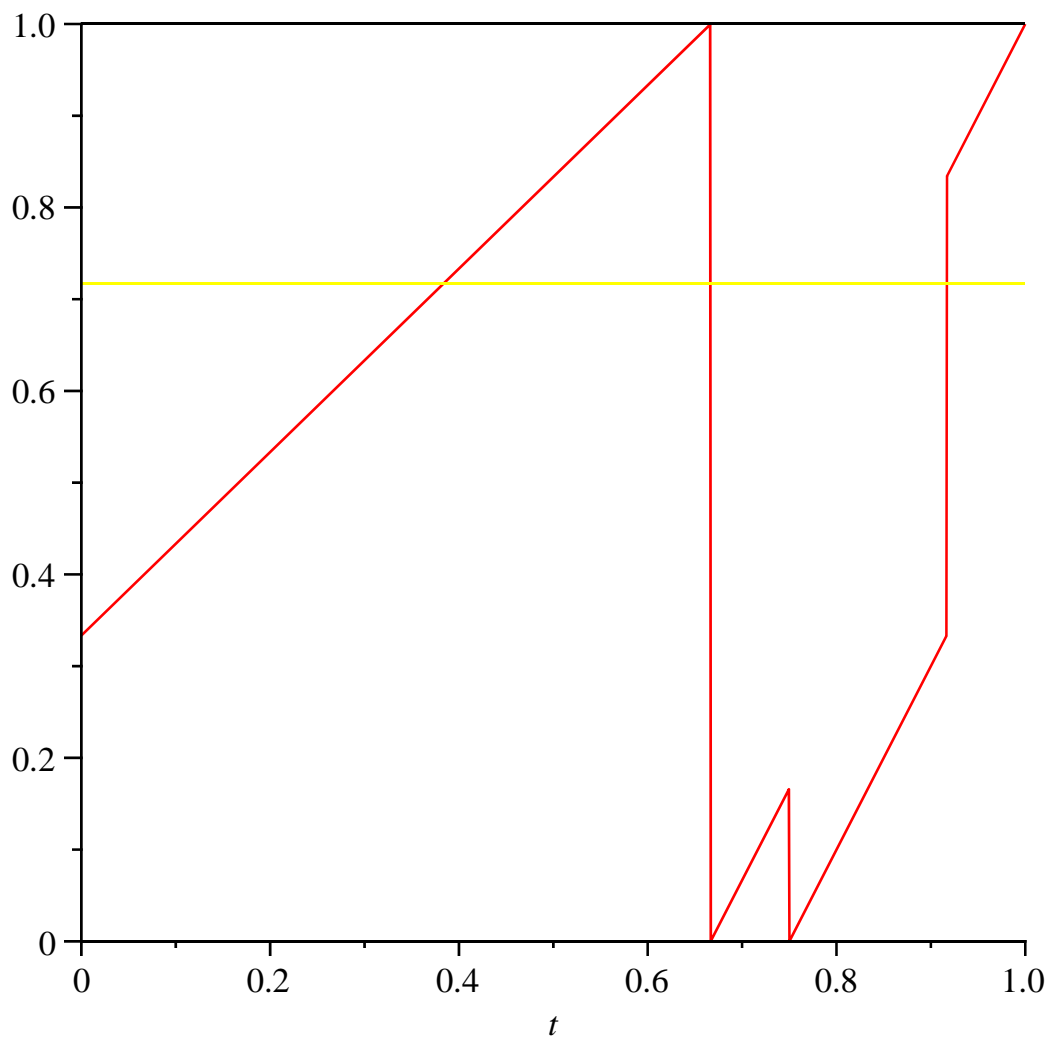
$err_5 := 1.000001745 \cdot 10^{-10}$



$su := 0$

1

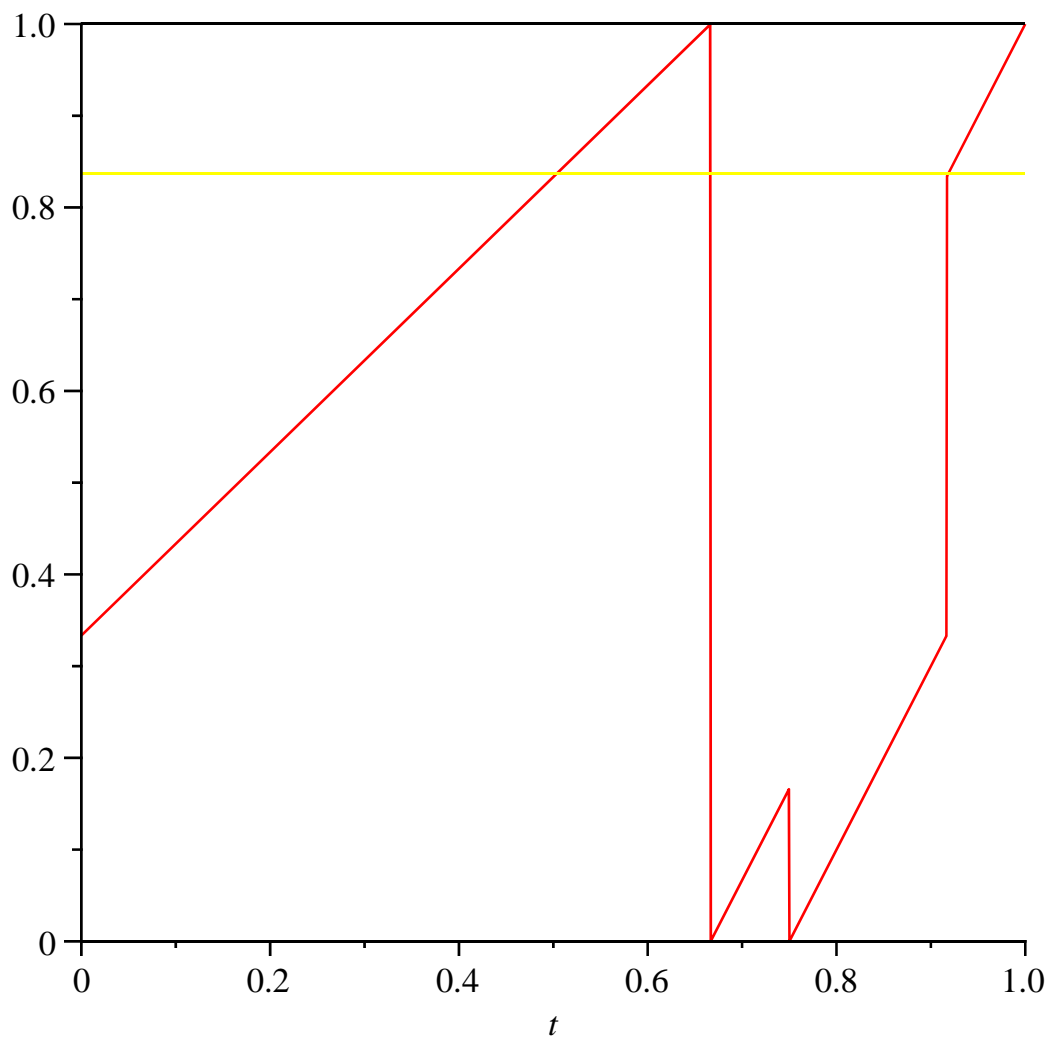
$err_6 := 1.000001745 \cdot 10^{-10}$



$su := 0$

1

$err_7 := 1.000001745 \cdot 10^{-10}$

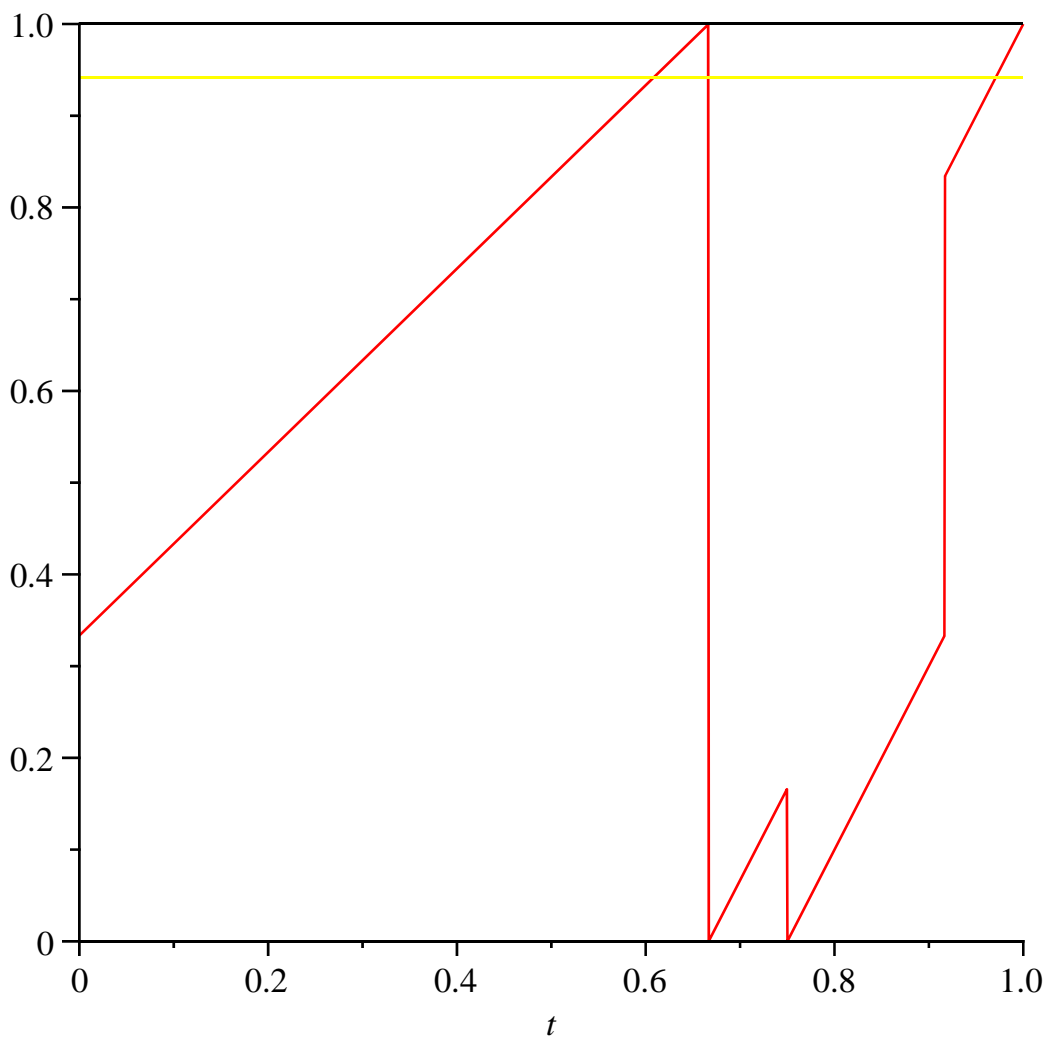


$su := 0$

1

4

$err_8 := 5.000034891 \cdot 10^{-11}$



$su := 0$

1

4

$err_0 := 5.000034891 \cdot 10^{-11}$

$y =, 0.0693953992$

$err[0, J] =, -2.000003489 \cdot 10^{-10}$

$y =, 0.1914298711$

$err[1, J] =, -1.500005234 \cdot 10^{-10}$

$y =, 0.2450147686$

$err[2, J] =, -1.500005234 \cdot 10^{-10}$

$y =, 0.3352263657$

$err[3, J] =, 1.000001745 \cdot 10^{-10}$

$y =, 0.4819571011$

$err[4, J] =, 1.000001745 \cdot 10^{-10}$

$y =, 0.5849634042$

$err[5, J] =, 1.000001745 \cdot 10^{-10}$

$y =, 0.6704117256$

$err[6, j] = 1.000001745 \cdot 10^{-10}$

$y = 0.7169276114$

$err[7, j] = 1.000001745 \cdot 10^{-10}$

$y = 0.8371184668$

$err[8, j] = 5.000034891 \cdot 10^{-11}$

$y = 0.9419107018$

$err[9, j] = 5.000034891 \cdot 10^{-11}$

