

Table of Laplace Transforms

$f(t) = \mathcal{L}^{-1}\{F(s)\}$	$F(s) = \mathcal{L}\{f(t)\} = \int_0^\infty e^{-st} f(t) dt$
1	$\frac{1}{s}, \ s > 0$
e^{at}	$\frac{1}{s-a}, \ s > a$
$t^n, \ n \text{ integer } > 0$	$\frac{n!}{s^{n+1}}, \ s > 0$
$t^p, \ p > -1$	$\frac{\Gamma(p+1)}{s^{p+1}}, \ s > 0$
$\sin(bt)$	$\frac{b}{s^2+b^2}, \ s > 0$
$\cos(bt)$	$\frac{s}{s^2+b^2}, \ s > 0$
$\sinh(bt)$	$\frac{b}{s^2-b^2}, \ s > b $
$\cosh(bt)$	$\frac{s}{s^2-b^2}, \ s > b $
$e^{at} \sin(bt)$	$\frac{b}{(s-a)^2+b^2}, \ s > a$
$e^{at} \cos(bt)$	$\frac{s-a}{(s-a)^2+b^2}, \ s > a$
$e^{at} f(t)$	$F(s-a), \ s > a$
$(-t)^n f(t), \ n \text{ integer } > 0$	$F^{(n)}(s)$
$f^{(n)}(t)$	$s^n F(s) - s^{n-1} f(0) - \dots - f^{(n-1)}(0)$
$f(ct)$	$\frac{1}{c} F\left(\frac{s}{c}\right), \ c > 0$
$u_c(t)$	$\frac{e^{-cs}}{s}, \ c \geq 0$
$u_c(t)f(t-c)$	$e^{-cs} F(s), \ c \geq 0$
$\delta(t-c)$	$e^{-cs}, \ c \geq 0$
$\int_0^t f(t-\tau)g(\tau)d\tau$	$F(s)G(s)$